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On the Feasibility and Suitability of MR Fluid Clutches in Human-Friendly Manipulators

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Abstract-An investigation into the suitability of magneto-4 rheological (MR) clutches in the context of developing feasible 5 6 actuation solutions for physical human-robot interaction is pre-7 sented. Contact and collision forces pose great danger to humans, and thus, the primary criteria for actuator development is safety. 8 While the majority of existing solutions make use of mechanical 9 compliance in some form, in this paper, we will approach the prob-10 11 lem by considering the use of MR clutches for coupling the motor 12 drive to the joint. The suitability of MR actuators to provide an intrinsically safe actuation platform is investigated by modeling 13 14 the torque to mass, and torque to inertia ratios, as well as output impedance of the MR clutch. These figures are compared to 15 16 commercially available servo motors as well as mechanically compliant based human-safe actuator models. The MR clutch is ana-17 lytically shown to have superior mass and inertia characteristics 18 over servo motors while either matching or surpassing the intrin-19 sic safety characteristics of the modeled compliant actuator. The 20 implementation of MR-clutch-based actuation systems is investi-21 gated by examining the distributed active semiactive approach. 22 23 The proposed approach is discussed in terms of mechanical as well controller complexity and relates the investigation to the fea-24 sibility of practical implementations. Performance characteristics 25 are empirically investigated by experimentation with a prototype 26 MR clutch constructed for this purpose. The prototype MR clutch 27 can transmit torque up to 75 Nm and has a bandwidth of 30 Hz. 28 Torque to mass and torque to inertia ratios of the prototype MR 29 clutch are substantially greater than that of comparable servo 30 motors. Conclusions drawn from this investigation indicate that 31 32 indeed MR clutch actuation approaches can be developed to balance safety and performance while maintaining reasonable system 33 complexity. 34

Index Terms-Human-robot interaction, magneto-rheological 35 (MR) fluids, safety and performance. 36

I. INTRODUCTION

NCREASINGLY, we are witnessing a growing number of 38 39 developments in the field of robotics characterized by their intent to integrate man and machine in a safe and functional

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manner [1]-[3]. The suitability of a manipulator to work in 40 close proximity with humans is determined first by the level of 41 safety it can guarantee toward its human counterparts. Guaran-42 teeing safety is a difficult if not impossible exercise as we can 43 rarely guarantee the dependability of the numerous components 44 required to complete a modern manipulator. Add in the human 45 factor, and our task becomes insurmountable. Thus, much fo-46 cus has been centered on interactive robots that are expected 47 to perform in a safe and dependable manner in unknown and 48 unpredictable environments. Collisions between robots and hu-49 mans constitute the primary safety concern. Such collisions are 50 responsible for numerous injuries each year [4], despite the ex-51 istence of barriers and other fail-safe mechanisms. As we move 52 closer toward a shared environment, new approaches to ma-53 nipulator design are becoming increasingly important. Devices 54 utilizing the unique properties of magneto-rheological (MR) 55 fluids have been developed for robotic applications, however, 56 almost entirely for use in haptic systems [5]–[9]. While it has 57 been suggested in the literature how such devices might be 58 used in a manipulator to improve both safety and performance 59 (i.e., [10], [11]), there appears to be a general reluctance toward 60 adopting such technology as a viable alternative to the current 61 solutions. 62

Control design and software issues for the manipulators in-63 tended to interact with humans also present a set of unique 64 challenges [12]. It is necessary to address safety, not only at the design, but at motion planning and control levels as well. Of high importance are identification and assessment of var-67 ious sources of danger [13]–[16] as well as obtaining simple 68 but realistic models of the environment and in particular of hu-69 mans [17], [18]. It is however, beyond the scope of this paper to 70 adequately discuss all subject matters. For more comprehensive 71 review of the software issues see [19]. 72

This paper is organized in seven sections. Section II briefly 73 discusses fundamental issues relating to actuator and manipu-74 lator design that have detrimental effects on safety, as well as 75 review the shortcomings of existing solutions. Section III re-76 views the construction and principles of the MR clutch, used to 77 develop MR actuators (MRAs). Section IV presents an investi-78 gation into MR clutch actuators' figures of merit to provide a 79 comparison to differing actuator types. In Section V, we propose 80 an elaborated MR-based actuation approach that leverages the 81 strengths highlighted in the previous section. The goals of the 82 proposed actuation approach are to maintain safe physical in-83 teractions with humans, while improving the performance over 84 existing human-safe actuation techniques. Section VI highlights 85 the results of performance validation experiments conducted on 86 a prototype MRA. Finally, concluding remarks are given in 87 Section VII. 88

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rigidly coupled to the input drive. Here, V_c is collision velocity.

II. HUMAN-FRIENDLY MANIPULATORS: BACKGROUND AND ANALYSIS

In attempts to guarantee the safety of humans within a shared 91 workspace, much research has been focused on the development 92 of manipulators which are intrinsically safe. That is, manipula-93 tors which by means of their mechanical properties can guaran-94 95 tee some level of collision safety in the absence of a controller. 96 To understand the degree of safety one might associate with a manipulator, we may look at the results of an uncontrolled col-97 lision through the use of the head injury criterion (HIC) [20]. 98 The HIC along with its variations have long been used by the 99 automotive industry to gauge the severity of collisions. In the 100 101 field of robotics, it can also be used to gain similar insight. The HIC is defined as 102

$$\text{HIC} = \max_{t_1, t_2} \left\{ (t_2 - t_1) \left(\frac{1}{t_2 - t_1} \int_{t_1}^{t_2} a(t) dt \right)^{2.5} \right\}$$
(1)

where a is the acceleration of the head (in g's), and t_1 and t_2 are 103 times within the collision selected to maximize the HIC, such 104 that $t_1 < t_2$. An HIC of 100 is the maximum value considered 105 to be nonlife threatening. To gauge how the effective inertia of 106 a link is related to a manipulator's inherent ability to collide 107 safely, we simulate a single-axis robot colliding with a human 108 head (see Fig. 1). As we may have expected, the results of the 109 HIC indicate that a manipulator's safety can be improved by 110 reducing its effective inertia. Thus, a generation of light-weight 111 manipulators was inspired. One of the first manipulators to be 112 designed under the light-weight paradigm was the whole arm 113 manipulator (WAM) [21]. The WAM uses steel cable trans-114 mission allowing actuators to be located at the manipulator's 115 base. Another successful implementation is the DLR-III [22]. 116 Using light-weight carbon composites to form its links as well 117 as advanced actuator design integrated with low-weight har-118 monic reduction gears, allows the DLR-III to attain a fully inte-119 grated light-weight design. These approaches however address 120 only half of the problem. Robotic manipulators make use of 121 high-performance servo motors to drive their links. These servo 122 motors produce low output torque, and at high velocity with 123 respect to what is suitable for most robots. To remedy this, gear-124 reduction systems are most commonly employed. The resulting 125 torque at the link is the actuator torque multiplied by the gear 126 ratio G_r , while the reflected actuator inertia associated with the 127 rotor of the motor is multiplied by G_r^2 . Thus, the effective inertia 128

experienced by a robotic link can be expressed as

$$J_e = J_\ell + G_r^2 J_r \tag{2}$$

where J_{ℓ} is the inertia of the link, and J_r is the rotor inertia 130 of the motor. The reflected actuator inertia of a manipulator 131 can in fact be much larger than that of the link [23], thereby 132 contributing a larger share of the inertial load during collisions. 133 In response to this, several novel actuation systems have been 134 proposed which work to decouple the reflected actuator inertia 135 from the link. Receiving considerable attention are actuation 136 systems that introduce compliance into their transmission. se-137 ries elastic actuator (SEA) [24] accomplishes precisely this by 138 integrating an elastic element between the motor and link. Intu-139 itively, lower coupling stiffness results in collisions producing 140 lower HIC values. The addition of the elastic element however 141 dramatically reduces the controllable bandwidth of the actua-142 tor [25]. The integration of SEA devices establish a trade-off 143 between safety and performance as a function of coupling stiff-144 ness. The variable stiffness actuator (VSA) [26] was developed 145 to address the stringent safety-performance trade-off character-146 ized by the SEA. Like the SEA, the VSA incorporates an elastic 147 element into its transmission. The VSA however can alter the 148 stiffness of the transmission coupling during task execution. It 149 can be observed from Fig. 1 that at lower velocities, collisions 150 involving stiff manipulators may still occur safely. By dynam-151 ically varying the stiffness to be compliant for high velocities, 152 and stiff at low velocities, performance can be improved while 153 maintaining safety. 154

Chew *et al.* [27] proposed the series damper actuator (SDA) 155 as a means of achieving force/torque control. The SDA is con-156 structed by placing a rotary damper in series with the motor 157 drive. Force/torque control is achieved by controlling the rela-158 tive angular velocity between the motor drive and the damper 159 output. Similar to the SEA, the SDA has inherent impact absorp-160 tion properties, which are attributed to the dissipative nature of 161 the series damper. Similarly to the addition of an elastic ele-162 ment, the SDA reduces the actuator bandwidth for decreasing 163 coupling viscosity. Again, a trade-off exists between safety and 164 performance, in this case parameterized by the damping coeffi-165 cient. (It should be noted that the authors of [27] suggest how 166 MR fluids can be used to vary the damping coefficient). Using a 167 damping element over an elastic element subsequently reduces 168 the order of the system by one. This implies that the SDA is 169 capable of achieving a larger force bandwidth over the SEA. 170

Variable impedance actuation (VIA) [28] combines both vari-171 able elastic and variable damping elements in the transmission. 172 This approach is an extension of the VSA concept. By being 173 able to vary both an elastic and a damping element, it is possible 174 to again recuperate performance during task execution while 175 guaranteeing the safety of humans. The VIA further requires 176 additional actuators to vary coupling parameters. 177

Another notable variation on the SEA is the distributed macro-178 mini actuation approach (DM^2) [23]. Actuation of the joint is 179 achieved by the coupling of a low-frequency high-torque SEA 180 with a high-frequency low-torque servo. The high-frequency 181 servo, directly coupled to the joint, is used to actuate the ma-182 nipulator in a complimentary frequency space to that of the 183

Fig. 1. Simulated HIC of a single-axis manipulator. The simulated link is



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Fig. 2. Cross section of a multidisk style MR clutch and its corresponding magnetic circuit.

SEA. In this way, the effective controllable bandwidth of the
manipulator is improved. The low-torque high-frequency servo
is selected such that its output inertia is minimized. Thus, safety
is maintained while performance is improved.

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III. MR CLUTCH

MR fluids are a suspension of micrometer-sized particles in a carrier fluid. When subjected to a magnetic field, the particles aggregate into columns aligned in the direction of the field. Subsequently, the columns act to resist shearing of the fluid perpendicular to the field. The apparent yield stress of the fluid is dependant on, and increases with the intensity of the applied field.

Fig. 2 is a cross section of a multidisk style MR fluid clutch. 196 MR fluid fills the volume between input and output disks. Rota-197 tion of the input shaft causes shearing in the fluid with respect 198 199 to the output shaft. By energizing the electromagnetic coil, a field is induced in the MR fluid altering its apparent viscosity. 200 The outer casing of the MR clutch acts as the magnetic flux path 201 required to complete the magnetic circuit. The Bingham vis-202 coplastic model is commonly used to represent the shear stress 203 of the fluid as a function of the applied field and shear rate [29]. 204 205 The model is given by

$$\tau = \tau_y(\mathbf{H}) + \eta \frac{dv}{dz}, \qquad \tau > \tau_y \tag{3}$$

where τ is the shear stress, τ_y is the field-dependent yield stress, 206 **H** is the applied magnetic field intensity, η is the newtonian 207 viscosity, and dv/dz is the velocity gradient in the direction of 208 the field. Applying the Bingham viscoplastic model to a clutch, 209 we define r as the radius from the rotational axis, and l_f as the 210 thickness of the fluid-filled gap between input and output disks. 211 212 In situations where $r \gg l_f$ for $r \in [R_1, R_2]$ (see to Fig. 2), the velocity gradient becomes constant. We can then rewrite (3) as 213

$$\tau = \tau_y(\mathbf{H}) + \eta \dot{\gamma}(r), \qquad \tau > \tau_y \tag{4}$$

214 where the shear rate $\dot{\gamma}$ is defined as

$$\dot{\gamma} = \frac{\omega r}{l_f} \tag{5}$$

Α.

and ω is the angular velocity between input and output shafts of the clutch. The torque produced by a circumferential element at a radius r is given by

$$dT = 2\pi r^2 \tau dr. \tag{6}$$

We define a clutch as having N output disks. Substituting (4) 218 into (6) and integrating across both faces of each output disk, 219 we arrive at 220

$$T = 2N \int_{R_1}^{R_2} 2\pi \left(\tau_y(\mathbf{H}) r^2 + \eta \frac{\omega r^3}{l_f} \right) dr$$

= $4N\pi \left(\frac{\tau_y(\mathbf{H}) (R_2^3 - R_1^3)}{3} + \frac{\eta \omega (R_2^4 - R_1^4)}{4l_f} \right)$ (7)

as the torque transmitted by an N-disk clutch. Data relating 221 the yield stress τ_{y} of a fluid to an applied field are generally 222 published by the manufacturer. The viscosity η of the carrier 223 fluid is typically in the range of 0.1–0.3 Pas. The maximum 224 torque transmission capability of an MR clutch is dependent on 225 the maximum yield stress the material can produce. MR fluids 226 exhibit saturation in their yield stress at high field strengths. This 227 is a result of the underlying physics, and limits the amount of 228 torque a particular MR fluid can transmit in clutch applications. 229 MR fluids can produce maximum yield stresses typically in the 230 range of 50-100 kPa [30] depending on their chemistry. MR 231 fluids respond to an applied field on the order of 1 ms. However, 232 the actuation response of an MR clutch becomes delayed due to 233 field propagation through the magnetic circuit [31]. 234

In Section II, we discussed the effects of actuator mass, output 237 inertia, and output impedance on safety. In this section, we will 238 present models relating torque to mass, torque to inertia, as well 239 as the output impedance of (MRA). 240

Several configurations exist in which MR clutches can be utilized to develop an actuation system. The simplest configuration utilizes a motor to drive an MR clutch, which in turn drives the joint. To generalize the discussion, we will consider simplified mechanical models of the MR clutch based on the model presented in Section III. Note that in this section, we define the actuator output to be the output of an MR clutch. 241

MRAs have the characteristic of replacing the reflected rotor 249 inertia of the motor with the reflected inertia of the clutch output 250 shaft and disks. The benefit of MRAs is their high torque to 251 output inertia ratio as compared to servo motors. To show this, 252 we approximate the radius of the output shaft to be equivalent 253 to R_1 . The moment of inertia of a single output disk, J_d is given 254 by 255

$$J_d = \frac{1}{2} \pi \rho_d l_d \left(R_2^4 - R_1^4 \right)$$
 (8)

where ρ_d is the mass density of the disk material, l_d is the 256 thickness of the disk (commonly between 0.5 to 1 mm), and 257 R_1 and R_2 define the minor and major radii, respectively, of 258 the output disk. If we consider the torque transmitted solely 259

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by the field-dependant yield stress of the MR fluid, the torquetransmission of a single disk is then given by

$$T_d = \frac{4}{3}\pi\tau_y \left(R_2^3 - R_1^3\right).$$
 (9)

Furthermore, if we consider R_1 to be small, i.e., $R_2 \gg R_1$, then the contribution of the shaft region to both (8) and (9) is also small. By allowing R_1 to equal zero, we can approximate the torque–inertia ratio of a single disk to be

$$\alpha = \frac{T_d}{J_d} = \frac{8}{3} \frac{\tau_y}{\rho_d l_d R_2}.$$
(10)

As observed, the ratio becomes less favorable as R_2 increases. 266 This however is not the final measure that dictates the actuators 267 suitability. To grasp the overall effects of increasing radius, and 268 hence, torque capacity, the reflected inertia at the joint should be 269 consider. The reason for this is that as radius increases along with 270 torque capacity, the gear ratio required to amplify the actuator's 271 torque decreases. As the actuator inertia multiplies the square 272 of the gear ratio to arrive at the reflected inertia at the joint, 273 the analysis becomes important. The reflected inertia of the MR 274 clutch at the manipulator joint is given by 275

$$J'_{c} = \frac{1}{2} \pi \rho_{d} l_{d} N \left(R_{2}^{4} - R_{1}^{4} \right) G_{r}^{2}$$
(11)

where we have included N to multiply the inertia by the number of disks in the clutch. The gear ratio G_r is defined as

$$G_r = \frac{T'_c}{T_c} \tag{12}$$

where T'_c is the desired torque at the joint, and T_c is the output torque of the clutch. Rearranging (9) to show the outer radius R_2 as a function of the clutch output torque yields

$$R_2 = \left(\frac{3}{4}\frac{T_c}{\pi\tau_y N} + R_1^3\right)^{1/3}.$$
 (13)

We can then write (13) representing the reflected inertia of a MR clutch at the manipulator joint as a function of the clutch torque

$$J_c' = \frac{1}{2} \pi \rho_d l_d N \left(\left(\frac{3}{4} \frac{T_c}{\pi \tau_y N} + R_1^3 \right)^{4/3} - R_1^4 \right) \left(\frac{T_c'}{T_c} \right)^2.$$
(14)

Fig. 3 shows the values of reflected actuator inertia versus output torque for the MR clutch. The plot also includes equivalent values for commercially available low-inertia servo motors. It is evident that the MR clutch demonstrates superior output inertia characteristics over the low-inertia servo motors. We note that the developed torque to inertia relationship improves dramatically at larger values of output torque.

291 B. Mass of MR Clutch

In this section, we develop torque to mass relationships for the MR clutch. While the relationships are developed using simplified geometric models, they serve to establish the order in which the clutch mass compares to that of servo motors, as well as the rate at which clutch mass increases with respect to transmittable torque capacity. To develop a relationship between clutch mass



Fig. 3. Reflected inertia versus output torque for the MR clutch (see Table I) and commercially available low-inertia servo motors. ($T'_c = 50$ Nm).



Fig. 4. Simplified MR clutch model. The electromagnetic coil is contained between R_2 and R_3 , and R_4 defines the outer surface of the ferrous core.

and torque capacity for MR fluid clutches, we consider the simplified geometric model detailed in Fig. 4. We will solve for 299 required parametric values through the application of magnetic 300 circuit analysis. We divide the reluctance of the core \Re_c into 301 three sections, namely \Re_{c_1} , \Re_{c_2} , and \Re_{c_3} . The symmetric geometry of the model dictates the reluctance \Re_{c_2} to be equivalent 303 to that of \Re_{c_3} . Thus, we define the reluctance of the core to be 304

$$\Re_c = \Re_{c_1} + 2\,\Re_{c_{23}} \tag{15}$$

where $\Re_{c_{23}} = \Re_{c_2} = \Re_{c_3}$. We have defined a clutch by the num-305 ber of output disks N coupled to the output shaft. For N output 306 disks, a clutch is required to have N - 1 input disks, and a total 307 of 2N MR fluid interface gaps positioned between input and 308 output disks. In the simplified model of Fig. 4, we define both 309 geometric and material properties of the input and output disks 310 to be identical. The disk pack assembly thus contains 2N-1311 disks and 2N MR fluid interface gaps. The reluctance of the 312 disk pack assembly \Re_p can then be written as 313

$$\Re_p = (2N-1)\,\Re_d + 2N\,\Re_f \tag{16}$$

where \Re_d and \Re_f are the reluctance of a single disk and single 314 MR fluid interface gap, respectively. The reluctance of a material 315 is given by $\Re = l/(\mu_0 \mu_r A)$, where *l* is the mean length of the 316 flux path through the material, $\mu_0 = 4\pi \times 10^{-7}$ H/m is the 317 permeability of free space, μ_r is the relative permeability of 318 the material, and A is the cross-sectional area of the material 319 perpendicular to the flux path. Assuming that the mean flux path 320 through any of the circuit members lies at its geometric center, 321

 TABLE I

 PARAMETER VALUES FOR SIMPLIFIED MR CLUTCH MODEL

Parameter	Symbol	Value
Disk thickness Fluid gap thickness	l_d l_f	1.0 [mm] 0.5 [mm]
Disk minor radius Max operating yield stress Coil current density	$egin{array}{c} R_1 \ au_y^* \ J_w \end{array}$	10 [mm] 40 [kpa] 2.5 ×10 ⁶ [A/m ²]

we can then derive the reluctance of the individual componentsof the simplified clutch model to be

$$\Re_{c_{1}} = \frac{l_{p} + l_{c}}{\mu_{0}\mu_{r_{s}} \pi (R_{4}^{2} - R_{3}^{2})}$$
$$\Re_{c_{23}} = \int_{R_{2} + R_{1}/2}^{R_{4} + R_{3}/2} \frac{dr}{\mu_{0}\mu_{r_{s}} (2\pi r) l_{c}} = \frac{\ln (R_{4} + R_{3}/R_{2} + R_{1})}{2\mu_{0}\mu_{r_{s}} \pi l_{c}}$$
$$\Re_{d} = \frac{l_{d}}{\mu_{0}\mu_{r_{s}} \pi (R_{2}^{2} - R_{1}^{2})} \quad \Re_{f} = \frac{l_{f}}{\mu_{0}\mu_{r_{f}} \pi (R_{2}^{2} - R_{1}^{2})}.$$
 (17)

Here, μ_{r_s} is the permeability of steel, the material used for both the core and disks, μ_{r_f} is the permeability of the MR fluid, l_d is the thickness of a single disk, l_f is the distance between input and output disks forming the MR fluid gap, l_c is the thickness of the equivalent core sections, and $l_p = (2N - 1) l_d + 2N l_f$ is the length of the disk pack. The flux ϕ in the circuit is then given by

$$\phi = \frac{I}{\Re_c + \Re_p} = \frac{l_p (R_3 - R_2) J_w}{\Re_c + \Re_p}$$
(18)

where *I* is the total electric current through the cross section of the magnetic coil, and J_w is the current density of the coil cross section. The magnetic field intensity **H** at any point within the circuit is related to the circuit flux ϕ by

$$\mathbf{H} = \frac{\phi}{\mu_0 \mu_r A} \tag{19}$$

335 where again, μ_r and A are, respectively, the relative perme-336 ability and cross sectional area of the material at which the magnetic-field intensity H is to be determined. We now de-337 fine the parameter τ_u^* as the maximum yield stress at which 338 the MR fluid is to operate. Using data provided by the MR 339 340 fluid manufacturer relating the yield stress of the fluid to the applied magnetic field, we define \mathbf{H}^* as the magnetic-field in-341 tensity in the MR fluid required to produce the yield stress τ_y^* . 342 Rearranging (19), and substituting the appropriate MR fluid ge-343 ometric and material values, we define ϕ^* as the flux required 344 in the circuit to produce \mathbf{H}^* in the MR fluid 345

$$\phi^* = \mu_0 \mu_{r_f} \pi \left(R_2^2 - R_1^2 \right) \mathbf{H}^*.$$
(20)

346 R_2 is uniquely defined by the parameters T_c , N, R_1 , and τ_y^* 347 [refer to (13)]. Thus, for the given set of fixed parameters given 348 in Table I, we solve for the values of R_3 , R_4 , and l_c that satisfy (18) for $\phi = \phi^*$, while simultaneously minimizing the clutch



Fig. 5. Mass of simplified clutch models versus torque capacity (calculated using MR fluid characteristics of Lord Corp., MR-132DG MR fluid [32]).

mass
$$m_{MRC}$$
 given by
 $m_{MRC} = m_c + m_p + m_s + m_w$
 $m_c = \pi \left[\left(R_4^2 - R_3^2 \right) l_p + 2 \left(R_4^2 - R_1^2 \right) l_c \right] \rho_s$
 $m_p = \pi \left[(2N - 1) l_d \rho_s + 2N l_f \rho_f \right] \left(R_2^2 - R_1^2 \right)$
 $m_w = \pi \left(R_3^2 - R_2^2 \right) l_p \rho_{cu}$ $m_s = \pi R_1^2 \left(l_p + 2 l_c \right) \rho_{al}$
(21)

where m_c is the mass of the core, m_p is the mass of the disk pack 350 351 assembly which includes the MR fluid, m_s is the mass of the shaft, and m_w is the mass of the magnetic coil. In (21), ρ_s , ρ_f , 352 $\rho_{\rm cu}$, and $\rho_{\rm al}$ are the mass densities of steel, MR fluid, copper, 353 and aluminum, respectively. Fig. 5 shows the torque to mass 354 relationship of the simplified MR clutch model and compares it 355 to a commercially available servo motor. We note that due to the 356 mass overhead associated with the material required to form the 357 magnetic circuit, the torque to mass ratio of the MR clutch is 358 less favorable at very low values N. In the developed model, we 359 observe superior characteristics over the commercially available 360 servo motor. 361

C. Output Impedance

The output impedance of an actuator can be defined as

$$Z(s) = \frac{F_l(s)}{X_l(s)} \tag{22}$$

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where $F_l(s)$ is the force experienced by the load and $X_l(s)$ 364 is the displacement of the load. Actuators that limit or reduce 365 their impedance, especially at higher frequencies, offer a higher 366 degree of safety over those that do not. Within the controllable 367 bandwidth, impedance can be actively reduced by control ac-368 tion. However, above the controllable bandwidth, the impedance 369 is dominated by the open-loop characteristics of the actuator and 370 link. To form a comparison of the intrinsic properties of human 371 safe actuators, we consider the output impedance in the absence 372 of control. This is intended to represent the open-loop char-373 acteristics resulting from collisions occurring above the control 374 bandwidth. Fig. 6 shows a schematic representation of the MRA 375 and SEA models under consideration here. In this scenario, both 376



Fig. 6. Model schematic of unpowered (a) MRA, and (b) SEA.

377 motor and clutch are unpowered, allowing us to model the clutch 378 as a damper and inertial load. J_m is the inertia of the motor for both the MRA and SEA, K is the spring constant of the SEA, 379 B'_c is the damping coefficient of the MR clutch reflected to the 380 link, J'_c is the output inertia of the MR clutch reflected to the 381 link, and J_{ℓ} is the inertia of the link. The damping coefficient 382 383 in the MR clutch is determined by the Newtonian viscosity of the MR fluid (the viscosity at zero field) as well as the clutch 384 geometry. The output impedance of the SEA is given by 385

$$Z_{\rm SEA} = J_{\ell} s^2 + \frac{K J_m s^2}{J_m s^2 + K}.$$
 (23)

The value of the link inertia J_{ℓ} for the purpose of discussing the 386 387 characteristics of the SEA is somewhat arbitrary, and it is, thus, not uncommon to disregard it (allowing J_{ℓ} to equal zero). This 388 results in the properties of the SEA being characterized by the 389 second term only. In this circumstance, the output impedance 390 approaches the value of the spring constant K at high frequen-391 cies. It is this property of the SEA to limit output impedance 392 above the controllable bandwidth that intrinsically insures safe 393 interaction forces as well as impact loads. The output impedance 394 of the MRA is given as 395

$$Z_{\rm MRA} = (J_c' + J_\ell) \, s^2 + \frac{B_c' J_m s^2}{J_m s + B_c'}.$$
 (24)

A fair comparison would dictate if we once more disregard the 396 link inertia J_{ℓ} . While the second term increases (approximately) Q3 397 proportional to the reflected damping coefficient B'_c , at higher 398 399 frequencies it is the reflected inertia of the clutch J'_{c} in the first term that dominates the dynamics of the output impedance. 400 Noting that the output impedance of the MRA is not limited, 401 but rather continues to grow at high frequencies, seemingly, it 402 would not appear that the MRA poses the intrinsic safety char-403 acteristics of the SEA. However, to fairly evaluate the deficiency 404 of the MRA in this respect, it is instructive to consider practi-405 cal examples to establish the context in which the SEA offers 406 superior safety. If we reconsider the actuator models to include 407 the inertia of the link, for both the SEA and MRA, the inertial 408 impedance represented in the first terms will dominate the out-409 put impedances at higher frequencies. The output impedance 410 of the MRA can thus approach that of the SEA if $J'_{c} \ll J_{\ell}$. To 411 demonstrate the conditions in which we can satisfy $J'_c \ll J_\ell$, 412 we consider an applications requiring 50 Nm at the link. From 413 the values presented in Fig. 3, we can expect that the reflected 414 inertia of an MRA satisfying the 50-Nm requirement, would 415 be on the order of 10^{-3} kg m². We may then prescribe a lower 416 bound link inertia on the order of $J_{\ell} = 10^{-2} \text{ kg m}^2$, and one 417 order of magnitude larger than J'_c , the result of which being 418 that $(J_{\ell} + J'_{c}) \approx J_{\ell}$. To put the values into perspective, we can 419 express this lower bound as a link modeled by a point mass of 420



Fig. 7. Simulated output impedance for SEA and MRA. Values obtained from experimental MRA setup: $J_m = 26.9 \text{ kg m}^2$; $J'_c = 5 \times 10^{-3} \text{ kg m}^2$; $J_\ell = 0.045 \text{ kg m}^2$; $B = 0.1296 \text{ Ns m}^{-1}$. MRA produces 75-Nm output.



Fig. 8. DASA: solid line represents single clutch configuration, dotted line represents connection to second clutch present only in antagonistic configuration.

250 g at a radius of 20 cm. Links having inertias above this lower 421 bound could then be driven by either MRA or SEA and exhibit 422 nearly identical inertial impedances. In the application region of 423 50 Nm, it is reasonable to expect that most links will have inertias 424 larger than our defined lower bound. The implication being that 425 an SEA would not provide a safety improvement over an MRA 426 in the stated application region. It must be pointed out that we 427 have assumed the values presented in Fig. 3, which have been 428 computed from idealized models, are realistically achievable. 429 Fig. 7 shows simulated output impedances for both an MRA 430 and SEA. Values for the motor, MR clutch, and link inertias, as 431 well as clutch damping coefficient were obtained from an ex-432 perimental MRA setup (discussed later in greater detail). Using 433 these values, the output impedance of the MRA is simulated and 434 compared to that of an SEA. We see that in this circumstance, 435 the MRA demonstrates superior output impedance characteris-436 tics over that of the SEA. This is complimented by the superior 437 performance provided by the MRA. 438

V. DISTRIBUTED ACTIVE SEMIACTIVE ACTUATION 439

In this section, we propose an actuation technique that lever-440 ages the unique properties of MRAs. The proposed technique 441 is unique in which we attempt to reconcile safety, performance, 442 and complexity into a feasible solution. The distributed active 443 semiactive (DASA) actuation approach locates a driving motor 444 (the active actuator) at the base of the robot, and a semiactive MR 445 clutch at the joint (see to Fig. 8). The gear ratios G_1 and G_2 are 446 balanced to give the desired mass, and reflected output inertia 447 at the link. Reducing G_1 reduces the requirements of the clutch 448 transmission torque, which thus reduces the mass of the clutch, 449 however, the reflected output inertia is inevitably increased as 450 G_2 must then be increased to compensate. In Section IV, we 451 have shown how actuating a joint via an MR clutch can reduce 452

mass and reflected output inertia over conventional servo mo-453 tors. The impact on safety is immediately appreciated as the 4**94** effective inertia of the link is instantly reduced. This not only 455 456 improves manipulator performance, but further allows a manipulator to operate at higher velocities while maintaining safe HIC 457 values in the event of a collision. Moreover, the clutch itself is 458 back drivable, and can be thought of as exhibiting the properties 459 of an ideal torque source. This is an important characteristic 460 for human-friendly actuators as it facilitates impedance control. 461 462 While motors themselves are also intrinsically back drivable, the high-ratio-gear reductions they require are often not. Thus, 463 highly performing low-weight robots, which implement low 464 mass motors at the expense of high-ratio-gear reductions rely 465 on torque sensors in the control loop to electronically implement 466 back-drivable behavior. MR clutches posses a superior torque 467 468 to mass ratios over their servo motor counterparts, and thus can be designed to require much lower reduction ratios, if not de-469 veloped as direct-drive components, either way retaining their 470 471 intrinsic back-drivability. MR clutches have the added benefit of uniform torque transmission independent of armature position, 472 473 unlike servo motors, which suffer from nonlinearities such as cogging torque. Relocating the driving motor to the base of a 474 robot in order to reduce the mass at the link is not a new concept. 475 However, it has been a restrictive practice as the newly required 476 477 transmission responsible for bringing mechanical power from the base to the joint has commonly introduced unwanted friction 478 and compliance, which have reduced performance, and compli-479 cated the control system. The DASA implementation however 480 can be controlled to operate in a region in which torque transmis-481 sion is relatively immune to perturbation in the relative angular 482 483 velocity ω within the clutch, effectively allowing the clutch to act as a mechanical power filter. This characteristic which will 484 be explained momentarily allows the DASA system to function 485 with less than ideal mechanical transmission while maintaining 486 the performance and characteristics of a "stiff" transmission at 487 the joint. To explain this, we consider that the Bingham 488 model is accurate for describing the rheology of the fluid for 489 shear stress τ above the field-dependent yield stress τ_{u} , as ex-490 pressed in (3). It is this "Bingham region" in which we wish the 491 clutch to operate in order to benefit from the aforementioned 492 characteristics. Below the yield stress τ_y , however, the fluid ex-493 hibits newtonian characteristics, i.e., to say that τ grows with a 494 nonnegligible proportionality to the shear rate $\dot{\gamma}$ (for a more in-495 depth analysis see [33]). We can thus attribute a field-dependant 496 shear rate threshold $\dot{\gamma}^*$ below, which the fluid exhibits newtonian 497 characteristics, and above which, the Bingham model applies. 498 To maintain the clutch in the Bingham region, the fluid at any 499 radius r within the clutch must maintain a shear rate above $\dot{\gamma}^*$. 500 To guarantee this condition, we define the field-dependant an-501 gular velocity ω^* , the threshold above which operation in the 502 Bingham region is ensured as 503

$$\omega^* = \frac{\dot{\gamma}^* l_f}{R_1}.$$
(25)

We come to (25) by rearranging (5) and substituting r with its minimum value R_1 , the critical radius at which the lowest shear rate $\dot{\gamma}$ occurs. The control strategy should therefore attempt to avoid entering the Newtonian region by controlling the motor 507 angular velocity ω_m to satisfy the condition 508

$$\omega_m | = |\omega_j - \omega^*| + \epsilon^* \tag{26}$$

where ω_j is the angular velocity of the joint, and ϵ^* is a field-509 dependant error margin selected to ensure that the dynamics of 510 the motor have enough time to react to quickly varying values of 511 ω_i . ϵ^* must be large enough to ensure $\omega \geq \omega^*$ under all dynamic 512 situations, however, exact calculation of ϵ^* may be difficult as 513 there is a reliance on empirical data associated with the dy-514 namics of the joint/link. Care must be taken, however, to avoid 515 unnecessary power dissipation, which for a clutch is defined as 516 $P_d = T\omega$. Because ω tracks $\omega^* + \epsilon^*$, the value selected for ϵ^* 517 cannot be arbitrarily large. Crossing into the Newtonian region 518 is required to alter the direction of the torque transmitted to 519 the link when utilizing a single clutch to implement the DASA 520 system. As the motor must change the direction of its output ro-521 tation, the clutch torque transmission momentarily enters a dead 522 zone. This has the potential of creating a substantial backlash 523 effect. 524

A. Antagonistic DASA

An antagonistic configuration of the DASA system (see 526 Fig. 8) is intended to increase performance, and rectify the short-527 comings of the single-clutch DASA configuration. The motor 528 drives the input to two clutches, however in opposite directions 529 with respect to one another. The antagonistic output of the two 530 clutches is coupled to the link. By energizing one of the two 531 clutches, torque can be transmitted in either the clockwise or 532 counterclockwise direction. Thus, the antagonistic configura-533 tion allows for torque transmission to the joint to alter direction 534 without altering the direction of the motor output, thereby, elimi-535 nating the backlash introduced by the single-clutch DASA. Such 536 devices have been developed with electro-rheological (ER) flu-537 ids [34]. Maintaining rotation of the motor shaft, the bandwidth 538 of the antagonistic-DASA output is limited by charging and dis-539 charging of the magnetic field required to activate the clutch. If 540 we label the two clutches of an antagonistic DASA assembly as 541 C_1 and C_2 , then the motor's angular velocity should track 542

$$\omega_m = \max\{|\omega_j - \omega_1^*|, |\omega_2^* - \omega_j|\} + \epsilon^*$$
(27)

to avoid entering the Newtonian region of operation in either clutch. ω_1^* , and ω_2^* are the angular velocity of the Bingham region thresholds for clutches C_1 and C_2 , respectively. Note that in our convention, clutch C_2 has its input reversed in direction with respect to clutch C_1 , i.e., 547

$$\omega_1 = \omega_j - \omega_m \qquad \omega_2 = \omega_j + \omega_m. \tag{28}$$

The torque production for an antagonistic-DASA system operating in the Bingham region is then given by 549

$$T_{\rm AD} = T_1(\mathbf{H}_1) + T_2(\mathbf{H}_2) - \frac{2\pi\eta|\omega_j|}{l_f} \left(R_2^4 - R_1^4 \right)$$
(29)



Fig. 9. Sectional views of prototype MR clutch.

where T_1 and T_2 are the field-dependant torques produced by clutches C_1 , and C_2 , respectively, given by

$$T_{i} = \frac{4\pi}{3} \tau_{y}(\mathbf{H}_{i}) \left(R_{2}^{3} - R_{1}^{3}\right) \operatorname{sgn}(\omega_{i}), \quad i = 1, 2$$
(30)

where \mathbf{H}_1 and \mathbf{H}_2 are the fields produced in clutches C_1 , and C_2 , respectively. Note that the individual viscous torque contributions of C_1 and C_2 negate each other at the joint when $\omega_j = 0$. Viscosity of this class of fluids does not always obey ideal models. The antagonistic configuration can mitigate some nonlinearities which would otherwise have to be compensated for by the controller.

559 VI. PERFORMANCE VALIDATION OF A PROTOTYPE MR CLUTCH

In this section, we present results obtained by experimen-560 tation with a prototype MR clutch which we have designed 561 and constructed (see Fig. 9). The configuration of the prototype 562 MR clutch deviates from the model of Section IV. The magnetic 563 coil of the prototype is located radially inward of the clutch pack 564 in a "coil-in" configuration, as opposed to the coil-out config-565 uration previously discussed. Coupling the coil to the output 566 shaft has the intended effect of reducing clutch mass, however 567 comes at the expense of increasing output inertia. Design of 568 the prototype clutch is partially automated using the optimiza-569 tion process discussed in Section IV-B, where model equations 570 have been updated to reflect the change in configuration. The 571 method returns values for the dimensional parameters that min-572 imize the clutch mass for a given design torque. The prototype 573 MR clutch was specified with a design torque of 120 Nm. The 574 dimensional parameters returned by the optimization process 575 were used as the basis for practical design. Table II compares 576 the output torque, inertia, and mass of the physical prototype 577 MR clutch to the optimized design model. A large discrepancy 578 exists between the modeled and actual torque. The discrepancy 579 results primarily due to deviations in the physical design from 580 the geometric model used in the optimization. Practical design 581 features required for fastening and wire access are omitted from 582 the model. The optimization produces geometries in which flux 583 members enter magnetic saturation at the magnitude of circuit 584 flux corresponding to the specified design torque of the clutch. 585 586 Removal of ferromagnetic material from the optimized geom-

TABLE II Comparison Between Prototype and Modeled MR Clutch, as Well as Commercially Available Servomotors

		Prototype MR Clutch		Servomotors	
	Coil-out	Model	Actual	Parker	Maxon
(n		SMH-100	EC60	
Output Torque[Nm]	75	120	75	6.0	0.83
Mass[kg]	2.8	4.7	4.5	4.7	2.5
Inertia×10 ³ [kg·m ²]	0.19	2.8	5.0	0.34	0.083
Reflected					
Inertia $\times 10^3 [\text{kg} \cdot \text{m}^2]^{\dagger}$	-	-	2.22	23.3	302
[†] Reflected torque $T' = T'$	50 Nm				

Reflected torque $T_c' = 50$ Nm.



Fig. 10. Experimental setup used to verify the prototype MR clutch.

etry subsequently results in premature saturation of the circuit, 587 limiting the output torque of the clutch. 588

Much of our analysis prior to this section is based on the coil-589 out configuration model of Section IV-B. To add perspective, we 590 compare this model to the prototype MR clutch. The values for 591 the coil-out configuration shown in Table II are produced with 592 the geometric model and procedure described in Section IV-B, 593 where the output torque is specified to match the constructed 594 MR clutch and not the design value. The coil-out model does 595 not consider any practical design requirements, such as bearings, 596 seals, and mechanical coupling of the disks. In this regard, the 597 model represents an ideal scenario, or baseline for the achievable 598 characteristics in its configuration. The comparison indicates 599 that there is room for improvement of the prototype MR clutch. 600 Ideally, mass could be reduced by a third, while the output inertia 601 might be improved by an order of magnitude. Table II compares 602 the prototype MR clutch to two commercially available servo 603 motors. The servo motors are chosen to have comparable mass to 604 the prototype MR clutch. The output inertia of the servo motors 605 are between one and two orders of magnitude lower than that 606 of the MR clutch. However, when we consider a hypothetical 607 application requiring a 50-Nm output, the prototype MR clutch 608 posses the more favorable reflected inertia by at least an order 609 of magnitude. 610

To assess its performance characteristics, the clutch is 611 mounted to an experimentation platform (see Fig. 10) that incorporates an angular encoder (Renishaw RM22I) to read the 613 position of the output shaft. A static load cell (Transducer Techniques SBO-1K) mounts to the output shaft for torque experiments. A servo motor (Maxon EC 60) provides the rotational input to the MR clutch. A PID controller is implemented on a 617



Fig. 11. Torque tracking of step reference.



Fig. 12. Frequency response of the prototype MR clutch.

desktop computer that communicates with the experimentation
platform via a National Instruments (NI USB-6229) multifunction I/O device. The output signal from the PID controller forms
the input signal to the current amplifier of the MR clutch, while
the rotational velocity of the motor is kept constant.

Fig. 11 shows the closed-loop response to a step input. The 623 rise time is determined to be approximately 10 ms. The fre-624 quency response and dynamic characteristics are examined by 625 measuring the torque response to a sinusoidal reference signal 626 and initiating a frequency sweep at 0.5 Hz. Fig. 12 shows the 627 frequency response of the system. The resulting 3-dB actuator O5 628 bandwidth is measured to be approximately 30 Hz. Fig. 13 629 presents a set of four time domain measurements from the 630 sweep. Beginning at 0.5 Hz, we note excellent overlay of the 631 measured signal with that of the command. As the reference fre-632 quency is increased toward and above the actuator bandwidth, 633 we note that the response remains very smooth and as well re-634 tains the shape of the command signal quite well. Clean and 635 predictable torque outputs are an asset to the development of 636 controls and sensorization schemes that are required to monitor 637 and control contact forces between manipulators and humans. 638

Trajectory tracking experiments were conducted using the 639 angular encoder to form the feedback signal. The motor output 640 was held at a constant rotational velocity. A 50-cm long arm 641 constructed of medium density plastic was coupled to the out-642 put shaft. A counter weight of approximately 2 kg was mounted 643 to the end of arm. The results shown in Fig. 14 indicate the ca-644 pacity of the MR clutch in this arrangement to achieve favorable 645 precision in position control tasks. Small fluctuation errors in 646 the static portions of the trajectory demonstrate the capability 647



Fig. 13. Torque tracking of a sinusoidal references at frequencies of 0.5, 4.0, 16.0, and 33.3 Hz (from top to bottom).



Fig. 14. Position tracking of a trajectory reference. The center plot magnifies the trajectory in the region marked by the dotted red bounding box.

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of the MR clutch to suppress fluctuations present in the input 648 drive. 649

MR fluids exhibit promising characteristics for applications 651 in robotics. Specifically, they are well-suited for actuation sys-652 tems developed to interact physically with humans. As we have 653 shown, MR-clutch-based actuators demonstrate excellent torque 654 to mass, and torque to inertia characteristics. This is especially 655 evident for clutches having large torque capacities. This cre-656 ates a niche opportunity for MR-based actuators to be devel-657 oped into light-weight direct-drive (DD) systems. Light-weight 658

DD systems exhibit several characteristics that are sought af-659 ter for human-friendly manipulators, namely: intrinsic back-660 drivability, low output inertia, superior performance and band-661 662 width, as well as high precision in the control of output torque. Furthermore, MR-based actuators can potentially reduce sys-663 tem complexity. Potentially, the accuracy of torque transmis-664 sion models in such systems could allow for high fidelity torque 665 control without the requirement for torque sensors at the joints. 666 This is in contrast to the increasingly complex actuation solu-667 668 tions proposed to deal with physical human interaction.

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On the Feasibility and Suitability of MR Fluid Clutches in Human-Friendly Manipulators

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Abstract-An investigation into the suitability of magneto-4 rheological (MR) clutches in the context of developing feasible 5 6 actuation solutions for physical human-robot interaction is pre-7 sented. Contact and collision forces pose great danger to humans, and thus, the primary criteria for actuator development is safety. 8 While the majority of existing solutions make use of mechanical 9 compliance in some form, in this paper, we will approach the prob-10 11 lem by considering the use of MR clutches for coupling the motor 12 drive to the joint. The suitability of MR actuators to provide an intrinsically safe actuation platform is investigated by modeling 13 14 the torque to mass, and torque to inertia ratios, as well as out-15 put impedance of the MR clutch. These figures are compared to 16 commercially available servo motors as well as mechanically compliant based human-safe actuator models. The MR clutch is ana-17 lytically shown to have superior mass and inertia characteristics 18 over servo motors while either matching or surpassing the intrin-19 sic safety characteristics of the modeled compliant actuator. The 20 implementation of MR-clutch-based actuation systems is investi-21 gated by examining the distributed active semiactive approach. 22 23 The proposed approach is discussed in terms of mechanical as well controller complexity and relates the investigation to the fea-24 sibility of practical implementations. Performance characteristics 25 are empirically investigated by experimentation with a prototype 26 MR clutch constructed for this purpose. The prototype MR clutch 27 can transmit torque up to 75 Nm and has a bandwidth of 30 Hz. 28 29 Torque to mass and torque to inertia ratios of the prototype MR clutch are substantially greater than that of comparable servo 30 motors. Conclusions drawn from this investigation indicate that 31 32 indeed MR clutch actuation approaches can be developed to balance safety and performance while maintaining reasonable system 33 complexity. 34

Index Terms—Human–robot interaction, magneto-rheological
 (MR) fluids, safety and performance.

I. INTRODUCTION

NCREASINGLY, we are witnessing a growing number of
 developments in the field of robotics characterized by their intent to integrate man and machine in a safe and functional

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manner [1]-[3]. The suitability of a manipulator to work in 40 close proximity with humans is determined first by the level of 41 safety it can guarantee toward its human counterparts. Guaran-42 teeing safety is a difficult if not impossible exercise as we can 43 rarely guarantee the dependability of the numerous components 44 required to complete a modern manipulator. Add in the human 45 factor, and our task becomes insurmountable. Thus, much fo-46 cus has been centered on interactive robots that are expected 47 to perform in a safe and dependable manner in unknown and 48 unpredictable environments. Collisions between robots and hu-49 mans constitute the primary safety concern. Such collisions are 50 responsible for numerous injuries each year [4], despite the ex-51 istence of barriers and other fail-safe mechanisms. As we move 52 closer toward a shared environment, new approaches to ma-53 nipulator design are becoming increasingly important. Devices 54 utilizing the unique properties of magneto-rheological (MR) 55 fluids have been developed for robotic applications, however, 56 almost entirely for use in haptic systems [5]–[9]. While it has 57 been suggested in the literature how such devices might be 58 used in a manipulator to improve both safety and performance 59 (i.e., [10], [11]), there appears to be a general reluctance toward 60 adopting such technology as a viable alternative to the current 61 solutions. 62

Control design and software issues for the manipulators in-63 tended to interact with humans also present a set of unique 64 challenges [12]. It is necessary to address safety, not only at 65 the design, but at motion planning and control levels as well. 66 Of high importance are identification and assessment of var-67 ious sources of danger [13]–[16] as well as obtaining simple 68 but realistic models of the environment and in particular of hu-69 mans [17], [18]. It is however, beyond the scope of this paper to 70 adequately discuss all subject matters. For more comprehensive 71 review of the software issues see [19]. 72

This paper is organized in seven sections. Section II briefly 73 discusses fundamental issues relating to actuator and manipu-74 lator design that have detrimental effects on safety, as well as 75 review the shortcomings of existing solutions. Section III re-76 views the construction and principles of the MR clutch, used to 77 develop MR actuators (MRAs). Section IV presents an investi-78 gation into MR clutch actuators' figures of merit to provide a 79 comparison to differing actuator types. In Section V, we propose 80 an elaborated MR-based actuation approach that leverages the 81 strengths highlighted in the previous section. The goals of the 82 proposed actuation approach are to maintain safe physical in-83 teractions with humans, while improving the performance over 84 existing human-safe actuation techniques. Section VI highlights 85 the results of performance validation experiments conducted on 86 a prototype MRA. Finally, concluding remarks are given in 87 Section VII. 88

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Fig. 1. Simulated HIC of a single-axis manipulator. The simulated link is rigidly coupled to the input drive. Here, V_c is collision velocity.

II. HUMAN-FRIENDLY MANIPULATORS: BACKGROUND AND ANALYSIS

In attempts to guarantee the safety of humans within a shared 91 workspace, much research has been focused on the development 92 of manipulators which are intrinsically safe. That is, manipula-93 tors which by means of their mechanical properties can guaran-94 95 tee some level of collision safety in the absence of a controller. 96 To understand the degree of safety one might associate with a manipulator, we may look at the results of an uncontrolled col-97 lision through the use of the head injury criterion (HIC) [20]. 98 The HIC along with its variations have long been used by the 99 automotive industry to gauge the severity of collisions. In the 100 101 field of robotics, it can also be used to gain similar insight. The HIC is defined as 102

$$\text{HIC} = \max_{t_1, t_2} \left\{ (t_2 - t_1) \left(\frac{1}{t_2 - t_1} \int_{t_1}^{t_2} a(t) dt \right)^{2,5} \right\}$$
(1)

where a is the acceleration of the head (in g's), and t_1 and t_2 are 103 times within the collision selected to maximize the HIC, such 104 that $t_1 < t_2$. An HIC of 100 is the maximum value considered 105 to be nonlife threatening. To gauge how the effective inertia of 106 a link is related to a manipulator's inherent ability to collide 107 safely, we simulate a single-axis robot colliding with a human 108 head (see Fig. 1). As we may have expected, the results of the 109 HIC indicate that a manipulator's safety can be improved by 110 reducing its effective inertia. Thus, a generation of light-weight 111 manipulators was inspired. One of the first manipulators to be 112 designed under the light-weight paradigm was the whole arm 113 manipulator (WAM) [21]. The WAM uses steel cable trans-114 mission allowing actuators to be located at the manipulator's 115 base. Another successful implementation is the DLR-III [22]. 116 Using light-weight carbon composites to form its links as well 117 as advanced actuator design integrated with low-weight har-118 monic reduction gears, allows the DLR-III to attain a fully inte-119 grated light-weight design. These approaches however address 120 only half of the problem. Robotic manipulators make use of 121 high-performance servo motors to drive their links. These servo 122 motors produce low output torque, and at high velocity with 123 respect to what is suitable for most robots. To remedy this, gear-124 reduction systems are most commonly employed. The resulting 125 torque at the link is the actuator torque multiplied by the gear 126 ratio G_r , while the reflected actuator inertia associated with the 127 rotor of the motor is multiplied by G_r^2 . Thus, the effective inertia 128

experienced by a robotic link can be expressed as

$$J_e = J_\ell + G_r^2 J_r \tag{2}$$

where J_{ℓ} is the inertia of the link, and J_r is the rotor inertia 130 of the motor. The reflected actuator inertia of a manipulator 131 can in fact be much larger than that of the link [23], thereby 132 contributing a larger share of the inertial load during collisions. 133 In response to this, several novel actuation systems have been 134 proposed which work to decouple the reflected actuator inertia 135 from the link. Receiving considerable attention are actuation 136 systems that introduce compliance into their transmission. se-137 ries elastic actuator (SEA) [24] accomplishes precisely this by 138 integrating an elastic element between the motor and link. Intu-139 itively, lower coupling stiffness results in collisions producing 140 lower HIC values. The addition of the elastic element however 141 dramatically reduces the controllable bandwidth of the actua-142 tor [25]. The integration of SEA devices establish a trade-off 143 between safety and performance as a function of coupling stiff-144 ness. The variable stiffness actuator (VSA) [26] was developed 145 to address the stringent safety-performance trade-off character-146 ized by the SEA. Like the SEA, the VSA incorporates an elastic 147 element into its transmission. The VSA however can alter the 148 stiffness of the transmission coupling during task execution. It 149 can be observed from Fig. 1 that at lower velocities, collisions 150 involving stiff manipulators may still occur safely. By dynam-151 ically varying the stiffness to be compliant for high velocities, 152 and stiff at low velocities, performance can be improved while 153 maintaining safety. 154

Chew *et al.* [27] proposed the series damper actuator (SDA) 155 as a means of achieving force/torque control. The SDA is con-156 structed by placing a rotary damper in series with the motor 157 drive. Force/torque control is achieved by controlling the rela-158 tive angular velocity between the motor drive and the damper 159 output. Similar to the SEA, the SDA has inherent impact absorp-160 tion properties, which are attributed to the dissipative nature of 161 the series damper. Similarly to the addition of an elastic ele-162 ment, the SDA reduces the actuator bandwidth for decreasing 163 coupling viscosity. Again, a trade-off exists between safety and 164 performance, in this case parameterized by the damping coeffi-165 cient. (It should be noted that the authors of [27] suggest how 166 MR fluids can be used to vary the damping coefficient). Using a 167 damping element over an elastic element subsequently reduces 168 the order of the system by one. This implies that the SDA is 169 capable of achieving a larger force bandwidth over the SEA. 170

Variable impedance actuation (VIA) [28] combines both variable elastic and variable damping elements in the transmission. 172 This approach is an extension of the VSA concept. By being 173 able to vary both an elastic and a damping element, it is possible 174 to again recuperate performance during task execution while 175 guaranteeing the safety of humans. The VIA further requires 176 additional actuators to vary coupling parameters. 177

Another notable variation on the SEA is the distributed macromini actuation approach (DM^2) [23]. Actuation of the joint is achieved by the coupling of a low-frequency high-torque SEA with a high-frequency low-torque servo. The high-frequency servo, directly coupled to the joint, is used to actuate the manipulator in a complimentary frequency space to that of the 183



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Fig. 2. Cross section of a multidisk style MR clutch and its corresponding magnetic circuit.

SEA. In this way, the effective controllable bandwidth of the
manipulator is improved. The low-torque high-frequency servo
is selected such that its output inertia is minimized. Thus, safety
is maintained while performance is improved.

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III. MR CLUTCH

MR fluids are a suspension of micrometer-sized particles in a carrier fluid. When subjected to a magnetic field, the particles aggregate into columns aligned in the direction of the field. Subsequently, the columns act to resist shearing of the fluid perpendicular to the field. The apparent yield stress of the fluid is dependant on, and increases with the intensity of the applied field.

Fig. 2 is a cross section of a multidisk style MR fluid clutch. 196 MR fluid fills the volume between input and output disks. Rota-197 tion of the input shaft causes shearing in the fluid with respect 198 199 to the output shaft. By energizing the electromagnetic coil, a field is induced in the MR fluid altering its apparent viscosity. 200 The outer casing of the MR clutch acts as the magnetic flux path 201 required to complete the magnetic circuit. The Bingham vis-202 coplastic model is commonly used to represent the shear stress 203 of the fluid as a function of the applied field and shear rate [29]. 204 205 The model is given by

$$\tau = \tau_y(\mathbf{H}) + \eta \frac{dv}{dz}, \qquad \tau > \tau_y \tag{3}$$

where τ is the shear stress, τ_y is the field-dependent yield stress, 206 **H** is the applied magnetic field intensity, η is the newtonian 207 viscosity, and dv/dz is the velocity gradient in the direction of 208 the field. Applying the Bingham viscoplastic model to a clutch, 209 we define r as the radius from the rotational axis, and l_f as the 210 thickness of the fluid-filled gap between input and output disks. 211 212 In situations where $r \gg l_f$ for $r \in [R_1, R_2]$ (see to Fig. 2), the velocity gradient becomes constant. We can then rewrite (3) as 213

$$\tau = \tau_y(\mathbf{H}) + \eta \dot{\gamma}(r), \qquad \tau > \tau_y \tag{4}$$

214 where the shear rate $\dot{\gamma}$ is defined as

$$\dot{\gamma} = \frac{\omega r}{l_f} \tag{5}$$

Α.

and ω is the angular velocity between input and output shafts of the clutch. The torque produced by a circumferential element at a radius r is given by

$$dT = 2\pi r^2 \tau dr. \tag{6}$$

We define a clutch as having N output disks. Substituting (4) 218 into (6) and integrating across both faces of each output disk, 219 we arrive at 220

$$T = 2N \int_{R_1}^{R_2} 2\pi \left(\tau_y(\mathbf{H}) r^2 + \eta \frac{\omega r^3}{l_f} \right) dr$$

= $4N\pi \left(\frac{\tau_y(\mathbf{H}) (R_2^3 - R_1^3)}{3} + \frac{\eta \omega (R_2^4 - R_1^4)}{4l_f} \right)$ (7)

as the torque transmitted by an N-disk clutch. Data relating 221 the yield stress τ_{y} of a fluid to an applied field are generally 222 published by the manufacturer. The viscosity η of the carrier 223 fluid is typically in the range of 0.1–0.3 Pas. The maximum 224 torque transmission capability of an MR clutch is dependent on 225 the maximum yield stress the material can produce. MR fluids 226 exhibit saturation in their yield stress at high field strengths. This 227 is a result of the underlying physics, and limits the amount of 228 torque a particular MR fluid can transmit in clutch applications. 229 MR fluids can produce maximum yield stresses typically in the 230 range of 50-100 kPa [30] depending on their chemistry. MR 231 fluids respond to an applied field on the order of 1 ms. However, 232 the actuation response of an MR clutch becomes delayed due to 233 field propagation through the magnetic circuit [31]. 234

In Section II, we discussed the effects of actuator mass, output 237 inertia, and output impedance on safety. In this section, we will 238 present models relating torque to mass, torque to inertia, as well 239 as the output impedance of (MRA). 240

MRAs have the characteristic of replacing the reflected rotor 249 inertia of the motor with the reflected inertia of the clutch output 250 shaft and disks. The benefit of MRAs is their high torque to 251 output inertia ratio as compared to servo motors. To show this, 252 we approximate the radius of the output shaft to be equivalent 253 to R_1 . The moment of inertia of a single output disk, J_d is given 254 by 255

$$J_d = \frac{1}{2} \pi \rho_d l_d \left(R_2^4 - R_1^4 \right)$$
 (8)

where ρ_d is the mass density of the disk material, l_d is the 256 thickness of the disk (commonly between 0.5 to 1 mm), and 257 R_1 and R_2 define the minor and major radii, respectively, of 258 the output disk. If we consider the torque transmitted solely 259

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by the field-dependant yield stress of the MR fluid, the torquetransmission of a single disk is then given by

$$T_d = \frac{4}{3}\pi\tau_y \left(R_2^3 - R_1^3\right).$$
 (9)

Furthermore, if we consider R_1 to be small, i.e., $R_2 \gg R_1$, then the contribution of the shaft region to both (8) and (9) is also small. By allowing R_1 to equal zero, we can approximate the torque–inertia ratio of a single disk to be

$$\alpha = \frac{T_d}{J_d} = \frac{8}{3} \frac{\tau_y}{\rho_d l_d R_2}.$$
(10)

As observed, the ratio becomes less favorable as R_2 increases. 266 This however is not the final measure that dictates the actuators 267 suitability. To grasp the overall effects of increasing radius, and 268 hence, torque capacity, the reflected inertia at the joint should be 269 consider. The reason for this is that as radius increases along with 270 torque capacity, the gear ratio required to amplify the actuator's 271 torque decreases. As the actuator inertia multiplies the square 272 of the gear ratio to arrive at the reflected inertia at the joint, 273 the analysis becomes important. The reflected inertia of the MR 274 clutch at the manipulator joint is given by 275

$$J'_{c} = \frac{1}{2} \pi \rho_{d} l_{d} N \left(R_{2}^{4} - R_{1}^{4} \right) G_{r}^{2}$$
(11)

where we have included N to multiply the inertia by the number of disks in the clutch. The gear ratio G_r is defined as

$$G_r = \frac{T'_c}{T_c} \tag{12}$$

where T'_c is the desired torque at the joint, and T_c is the output torque of the clutch. Rearranging (9) to show the outer radius R_2 as a function of the clutch output torque yields

$$R_2 = \left(\frac{3}{4}\frac{T_c}{\pi\tau_y N} + R_1^3\right)^{1/3}.$$
 (13)

We can then write (13) representing the reflected inertia of a MR clutch at the manipulator joint as a function of the clutch torque

$$J_c' = \frac{1}{2} \pi \rho_d l_d N \left(\left(\frac{3}{4} \frac{T_c}{\pi \tau_y N} + R_1^3 \right)^{4/3} - R_1^4 \right) \left(\frac{T_c'}{T_c} \right)^2.$$
(14)

Fig. 3 shows the values of reflected actuator inertia versus output torque for the MR clutch. The plot also includes equivalent values for commercially available low-inertia servo motors. It is evident that the MR clutch demonstrates superior output inertia characteristics over the low-inertia servo motors. We note that the developed torque to inertia relationship improves dramatically at larger values of output torque.

291 B. Mass of MR Clutch

In this section, we develop torque to mass relationships for the MR clutch. While the relationships are developed using simplified geometric models, they serve to establish the order in which the clutch mass compares to that of servo motors, as well as the rate at which clutch mass increases with respect to transmittable torque capacity. To develop a relationship between clutch mass



Fig. 3. Reflected inertia versus output torque for the MR clutch (see Table I) and commercially available low-inertia servo motors. ($T'_c = 50$ Nm).



Fig. 4. Simplified MR clutch model. The electromagnetic coil is contained between R_2 and R_3 , and R_4 defines the outer surface of the ferrous core.

and torque capacity for MR fluid clutches, we consider the simplified geometric model detailed in Fig. 4. We will solve for 299 required parametric values through the application of magnetic 300 circuit analysis. We divide the reluctance of the core \Re_c into 301 three sections, namely \Re_{c_1} , \Re_{c_2} , and \Re_{c_3} . The symmetric geometry of the model dictates the reluctance \Re_{c_2} to be equivalent 303 to that of \Re_{c_3} . Thus, we define the reluctance of the core to be 304

$$\Re_c = \Re_{c_1} + 2\,\Re_{c_{23}} \tag{15}$$

where $\Re_{c_{23}} = \Re_{c_2} = \Re_{c_3}$. We have defined a clutch by the num-305 ber of output disks N coupled to the output shaft. For N output 306 disks, a clutch is required to have N - 1 input disks, and a total 307 of 2N MR fluid interface gaps positioned between input and 308 output disks. In the simplified model of Fig. 4, we define both 309 geometric and material properties of the input and output disks 310 to be identical. The disk pack assembly thus contains 2N-1311 disks and 2N MR fluid interface gaps. The reluctance of the 312 disk pack assembly \Re_p can then be written as 313

$$\Re_p = (2N-1)\,\Re_d + 2N\,\Re_f \tag{16}$$

where \Re_d and \Re_f are the reluctance of a single disk and single 314 MR fluid interface gap, respectively. The reluctance of a material 315 is given by $\Re = l/(\mu_0 \mu_r A)$, where *l* is the mean length of the 316 flux path through the material, $\mu_0 = 4\pi \times 10^{-7}$ H/m is the 317 permeability of free space, μ_r is the relative permeability of 318 the material, and A is the cross-sectional area of the material 319 perpendicular to the flux path. Assuming that the mean flux path 320 through any of the circuit members lies at its geometric center, 321

 TABLE I

 PARAMETER VALUES FOR SIMPLIFIED MR CLUTCH MODEL

Parameter	Symbol	Value
Disk thickness Fluid gap thickness	l_d l_f	1.0 [mm] 0.5 [mm]
Disk minor radius Max operating yield stress Coil current density	$egin{array}{c} R_1 \ au_y^* \ J_w \end{array}$	10 [mm] 40 [kpa] 2.5 ×10 ⁶ [A/m ²]

we can then derive the reluctance of the individual componentsof the simplified clutch model to be

$$\Re_{c_{1}} = \frac{l_{p} + l_{c}}{\mu_{0}\mu_{r_{s}} \pi (R_{4}^{2} - R_{3}^{2})}$$
$$\Re_{c_{23}} = \int_{R_{2} + R_{1}/2}^{R_{4} + R_{3}/2} \frac{dr}{\mu_{0}\mu_{r_{s}} (2\pi r) l_{c}} = \frac{\ln (R_{4} + R_{3}/R_{2} + R_{1})}{2\mu_{0}\mu_{r_{s}} \pi l_{c}}$$
$$\Re_{d} = \frac{l_{d}}{\mu_{0}\mu_{r_{s}} \pi (R_{2}^{2} - R_{1}^{2})} \quad \Re_{f} = \frac{l_{f}}{\mu_{0}\mu_{r_{f}} \pi (R_{2}^{2} - R_{1}^{2})}.$$
 (17)

Here, μ_{r_s} is the permeability of steel, the material used for both the core and disks, μ_{r_f} is the permeability of the MR fluid, l_d is the thickness of a single disk, l_f is the distance between input and output disks forming the MR fluid gap, l_c is the thickness of the equivalent core sections, and $l_p = (2N - 1) l_d + 2N l_f$ is the length of the disk pack. The flux ϕ in the circuit is then given by

$$\phi = \frac{I}{\Re_c + \Re_p} = \frac{l_p (R_3 - R_2) J_w}{\Re_c + \Re_p}$$
(18)

where *I* is the total electric current through the cross section of the magnetic coil, and J_w is the current density of the coil cross section. The magnetic field intensity **H** at any point within the circuit is related to the circuit flux ϕ by

$$\mathbf{H} = \frac{\phi}{\mu_0 \mu_r A} \tag{19}$$

335 where again, μ_r and A are, respectively, the relative perme-336 ability and cross sectional area of the material at which the magnetic-field intensity H is to be determined. We now de-337 fine the parameter τ_u^* as the maximum yield stress at which 338 the MR fluid is to operate. Using data provided by the MR 339 fluid manufacturer relating the yield stress of the fluid to the 340 applied magnetic field, we define \mathbf{H}^* as the magnetic-field in-341 tensity in the MR fluid required to produce the yield stress τ_u^* . 342 Rearranging (19), and substituting the appropriate MR fluid ge-343 ometric and material values, we define ϕ^* as the flux required 344 in the circuit to produce \mathbf{H}^* in the MR fluid 345

$$\phi^* = \mu_0 \mu_{r_f} \pi \left(R_2^2 - R_1^2 \right) \mathbf{H}^*.$$
(20)

346 R_2 is uniquely defined by the parameters T_c , N, R_1 , and τ_y^* 347 [refer to (13)]. Thus, for the given set of fixed parameters given 348 in Table I, we solve for the values of R_3 , R_4 , and l_c that satisfy (18) for $\phi = \phi^*$, while simultaneously minimizing the clutch



Fig. 5. Mass of simplified clutch models versus torque capacity (calculated using MR fluid characteristics of Lord Corp., MR-132DG MR fluid [32]).

mass
$$m_{MRC}$$
 given by
 $m_{MRC} = m_c + m_p + m_s + m_w$
 $m_c = \pi \left[\left(R_4^2 - R_3^2 \right) l_p + 2 \left(R_4^2 - R_1^2 \right) l_c \right] \rho_s$
 $m_p = \pi \left[(2N - 1) l_d \rho_s + 2N l_f \rho_f \right] \left(R_2^2 - R_1^2 \right)$
 $m_w = \pi \left(R_3^2 - R_2^2 \right) l_p \rho_{cu}$ $m_s = \pi R_1^2 \left(l_p + 2 l_c \right) \rho_{al}$
(21)

where m_c is the mass of the core, m_p is the mass of the disk pack 350 assembly which includes the MR fluid, m_s is the mass of the 351 shaft, and m_w is the mass of the magnetic coil. In (21), ρ_s , ρ_f , 352 $\rho_{\rm cu}$, and $\rho_{\rm al}$ are the mass densities of steel, MR fluid, copper, 353 and aluminum, respectively. Fig. 5 shows the torque to mass 354 relationship of the simplified MR clutch model and compares it 355 to a commercially available servo motor. We note that due to the 356 mass overhead associated with the material required to form the 357 magnetic circuit, the torque to mass ratio of the MR clutch is 358 less favorable at very low values N. In the developed model, we 359 observe superior characteristics over the commercially available 360 servo motor. 361

C. Output Impedance

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The output impedance of an actuator can be defined as

$$Z(s) = \frac{F_l(s)}{X_l(s)} \tag{22}$$

where $F_l(s)$ is the force experienced by the load and $X_l(s)$ 364 is the displacement of the load. Actuators that limit or reduce 365 their impedance, especially at higher frequencies, offer a higher 366 degree of safety over those that do not. Within the controllable 367 bandwidth, impedance can be actively reduced by control ac-368 tion. However, above the controllable bandwidth, the impedance 369 is dominated by the open-loop characteristics of the actuator and 370 link. To form a comparison of the intrinsic properties of human 371 safe actuators, we consider the output impedance in the absence 372 of control. This is intended to represent the open-loop char-373 acteristics resulting from collisions occurring above the control 374 bandwidth. Fig. 6 shows a schematic representation of the MRA 375 and SEA models under consideration here. In this scenario, both 376



Fig. 6. Model schematic of unpowered (a) MRA, and (b) SEA.

motor and clutch are unpowered, allowing us to model the clutch 377 378 as a damper and inertial load. J_m is the inertia of the motor for both the MRA and SEA, K is the spring constant of the SEA, 379 B'_c is the damping coefficient of the MR clutch reflected to the 380 link, J'_c is the output inertia of the MR clutch reflected to the 381 link, and J_{ℓ} is the inertia of the link. The damping coefficient 382 383 in the MR clutch is determined by the Newtonian viscosity of the MR fluid (the viscosity at zero field) as well as the clutch 384 geometry. The output impedance of the SEA is given by 385

$$Z_{\rm SEA} = J_{\ell} s^2 + \frac{K J_m s^2}{J_m s^2 + K}.$$
 (23)

The value of the link inertia J_{ℓ} for the purpose of discussing the 386 387 characteristics of the SEA is somewhat arbitrary, and it is, thus, not uncommon to disregard it (allowing J_{ℓ} to equal zero). This 388 results in the properties of the SEA being characterized by the 389 second term only. In this circumstance, the output impedance 390 approaches the value of the spring constant K at high frequen-391 cies. It is this property of the SEA to limit output impedance 392 above the controllable bandwidth that intrinsically insures safe 393 interaction forces as well as impact loads. The output impedance 394 of the MRA is given as 395

$$Z_{\rm MRA} = (J_c' + J_\ell) s^2 + \frac{B_c' J_m s^2}{J_m s + B_c'}.$$
 (24)

A fair comparison would dictate if we once more disregard the 396 link inertia J_{ℓ} . While the second term increases (approximately) Q3 397 proportional to the reflected damping coefficient B'_c , at higher 398 399 frequencies it is the reflected inertia of the clutch J'_c in the first term that dominates the dynamics of the output impedance. 400 Noting that the output impedance of the MRA is not limited, 401 402 but rather continues to grow at high frequencies, seemingly, it would not appear that the MRA poses the intrinsic safety char-403 acteristics of the SEA. However, to fairly evaluate the deficiency 404 of the MRA in this respect, it is instructive to consider practi-405 cal examples to establish the context in which the SEA offers 406 superior safety. If we reconsider the actuator models to include 407 the inertia of the link, for both the SEA and MRA, the inertial 408 impedance represented in the first terms will dominate the out-409 put impedances at higher frequencies. The output impedance 410 of the MRA can thus approach that of the SEA if $J'_{c} \ll J_{\ell}$. To 411 demonstrate the conditions in which we can satisfy $J'_c \ll J_\ell$, 412 we consider an applications requiring 50 Nm at the link. From 413 the values presented in Fig. 3, we can expect that the reflected 414 inertia of an MRA satisfying the 50-Nm requirement, would 415 be on the order of 10^{-3} kg m². We may then prescribe a lower 416 bound link inertia on the order of $J_{\ell} = 10^{-2} \text{ kg m}^2$, and one 417 order of magnitude larger than J'_c , the result of which being 418 that $(J_{\ell} + J'_{c}) \approx J_{\ell}$. To put the values into perspective, we can 419 express this lower bound as a link modeled by a point mass of 420



Fig. 7. Simulated output impedance for SEA and MRA. Values obtained from experimental MRA setup: $J_m = 26.9 \text{ kg m}^2$; $J'_c = 5 \times 10^{-3} \text{ kg m}^2$; $J_\ell = 0.045 \text{ kg m}^2$; $B = 0.1296 \text{ Ns m}^{-1}$. MRA produces 75-Nm output.



Fig. 8. DASA: solid line represents single clutch configuration, dotted line represents connection to second clutch present only in antagonistic configuration.

250 g at a radius of 20 cm. Links having inertias above this lower 421 bound could then be driven by either MRA or SEA and exhibit 422 nearly identical inertial impedances. In the application region of 423 50 Nm, it is reasonable to expect that most links will have inertias 424 larger than our defined lower bound. The implication being that 425 an SEA would not provide a safety improvement over an MRA 426 in the stated application region. It must be pointed out that we 427 have assumed the values presented in Fig. 3, which have been 428 computed from idealized models, are realistically achievable. 429 Fig. 7 shows simulated output impedances for both an MRA 430 and SEA. Values for the motor, MR clutch, and link inertias, as 431 well as clutch damping coefficient were obtained from an ex-432 perimental MRA setup (discussed later in greater detail). Using 433 these values, the output impedance of the MRA is simulated and 434 compared to that of an SEA. We see that in this circumstance, 435 the MRA demonstrates superior output impedance characteris-436 tics over that of the SEA. This is complimented by the superior 437 performance provided by the MRA. 438

V. DISTRIBUTED ACTIVE SEMIACTIVE ACTUATION 439

In this section, we propose an actuation technique that lever-440 ages the unique properties of MRAs. The proposed technique 441 is unique in which we attempt to reconcile safety, performance, 442 and complexity into a feasible solution. The distributed active 443 semiactive (DASA) actuation approach locates a driving motor 444 (the active actuator) at the base of the robot, and a semiactive MR 445 clutch at the joint (see to Fig. 8). The gear ratios G_1 and G_2 are 446 balanced to give the desired mass, and reflected output inertia 447 at the link. Reducing G_1 reduces the requirements of the clutch 448 transmission torque, which thus reduces the mass of the clutch, 449 however, the reflected output inertia is inevitably increased as 450 G_2 must then be increased to compensate. In Section IV, we 451 have shown how actuating a joint via an MR clutch can reduce 452

mass and reflected output inertia over conventional servo mo-453 tors. The impact on safety is immediately appreciated as the 4**94** effective inertia of the link is instantly reduced. This not only 455 456 improves manipulator performance, but further allows a manipulator to operate at higher velocities while maintaining safe HIC 457 values in the event of a collision. Moreover, the clutch itself is 458 back drivable, and can be thought of as exhibiting the properties 459 of an ideal torque source. This is an important characteristic 460 for human-friendly actuators as it facilitates impedance control. 461 462 While motors themselves are also intrinsically back drivable, the high-ratio-gear reductions they require are often not. Thus, 463 highly performing low-weight robots, which implement low 464 mass motors at the expense of high-ratio-gear reductions rely 465 on torque sensors in the control loop to electronically implement 466 back-drivable behavior. MR clutches posses a superior torque 467 to mass ratios over their servo motor counterparts, and thus can 468 be designed to require much lower reduction ratios, if not de-469 veloped as direct-drive components, either way retaining their 470 intrinsic back-drivability. MR clutches have the added benefit of 471 uniform torque transmission independent of armature position, 472 473 unlike servo motors, which suffer from nonlinearities such as cogging torque. Relocating the driving motor to the base of a 474 robot in order to reduce the mass at the link is not a new concept. 475 However, it has been a restrictive practice as the newly required 476 477 transmission responsible for bringing mechanical power from the base to the joint has commonly introduced unwanted friction 478 and compliance, which have reduced performance, and compli-479 cated the control system. The DASA implementation however 480 can be controlled to operate in a region in which torque transmis-481 sion is relatively immune to perturbation in the relative angular 482 velocity ω within the clutch, effectively allowing the clutch to 483 act as a mechanical power filter. This characteristic which will 484 be explained momentarily allows the DASA system to function 485 with less than ideal mechanical transmission while maintaining 486 the performance and characteristics of a "stiff" transmission at 487 the joint. To explain this, we consider that the Bingham 488 model is accurate for describing the rheology of the fluid for 489 shear stress τ above the field-dependent yield stress τ_u , as ex-490 pressed in (3). It is this "Bingham region" in which we wish the 491 clutch to operate in order to benefit from the aforementioned 492 characteristics. Below the yield stress τ_y , however, the fluid ex-493 hibits newtonian characteristics, i.e., to say that τ grows with a 494 nonnegligible proportionality to the shear rate $\dot{\gamma}$ (for a more in-495 depth analysis see [33]). We can thus attribute a field-dependant 496 shear rate threshold $\dot{\gamma}^*$ below, which the fluid exhibits newtonian 497 characteristics, and above which, the Bingham model applies. 498 To maintain the clutch in the Bingham region, the fluid at any 499 radius r within the clutch must maintain a shear rate above $\dot{\gamma}^*$. 500 To guarantee this condition, we define the field-dependant an-501 gular velocity ω^* , the threshold above which operation in the 502 Bingham region is ensured as 503

$$\omega^* = \frac{\dot{\gamma}^* l_f}{R_1}.\tag{25}$$

We come to (25) by rearranging (5) and substituting r with its minimum value R_1 , the critical radius at which the lowest shear rate $\dot{\gamma}$ occurs. The control strategy should therefore attempt to avoid entering the Newtonian region by controlling the motor 507 angular velocity ω_m to satisfy the condition 508

$$\omega_m | = |\omega_j - \omega^*| + \epsilon^* \tag{26}$$

where ω_i is the angular velocity of the joint, and ϵ^* is a field-509 dependant error margin selected to ensure that the dynamics of 510 the motor have enough time to react to quickly varying values of 511 ω_j . ϵ^* must be large enough to ensure $\omega \ge \omega^*$ under all dynamic 512 situations, however, exact calculation of ϵ^* may be difficult as 513 there is a reliance on empirical data associated with the dy-514 namics of the joint/link. Care must be taken, however, to avoid 515 unnecessary power dissipation, which for a clutch is defined as 516 $P_d = T\omega$. Because ω tracks $\omega^* + \epsilon^*$, the value selected for ϵ^* 517 cannot be arbitrarily large. Crossing into the Newtonian region 518 is required to alter the direction of the torque transmitted to 519 the link when utilizing a single clutch to implement the DASA 520 system. As the motor must change the direction of its output ro-521 tation, the clutch torque transmission momentarily enters a dead 522 zone. This has the potential of creating a substantial backlash 523 effect. 524

A. Antagonistic DASA

An antagonistic configuration of the DASA system (see 526 Fig. 8) is intended to increase performance, and rectify the short-527 comings of the single-clutch DASA configuration. The motor 528 drives the input to two clutches, however in opposite directions 529 with respect to one another. The antagonistic output of the two 530 clutches is coupled to the link. By energizing one of the two 531 clutches, torque can be transmitted in either the clockwise or 532 counterclockwise direction. Thus, the antagonistic configura-533 tion allows for torque transmission to the joint to alter direction 534 without altering the direction of the motor output, thereby, elimi-535 nating the backlash introduced by the single-clutch DASA. Such 536 devices have been developed with electro-rheological (ER) flu-537 ids [34]. Maintaining rotation of the motor shaft, the bandwidth 538 of the antagonistic-DASA output is limited by charging and dis-539 charging of the magnetic field required to activate the clutch. If 540 we label the two clutches of an antagonistic DASA assembly as 541 C_1 and C_2 , then the motor's angular velocity should track 542

$$\omega_m = \max\{|\omega_j - \omega_1^*|, |\omega_2^* - \omega_j|\} + \epsilon^*$$
(27)

to avoid entering the Newtonian region of operation in either clutch. ω_1^* , and ω_2^* are the angular velocity of the Bingham region thresholds for clutches C_1 and C_2 , respectively. Note that in our convention, clutch C_2 has its input reversed in direction with respect to clutch C_1 , i.e., 547

$$\omega_1 = \omega_j - \omega_m \qquad \omega_2 = \omega_j + \omega_m. \tag{28}$$

The torque production for an antagonistic-DASA system operating in the Bingham region is then given by 549

$$T_{\rm AD} = T_1(\mathbf{H}_1) + T_2(\mathbf{H}_2) - \frac{2\pi\eta|\omega_j|}{l_f} \left(R_2^4 - R_1^4 \right)$$
(29)



Fig. 9. Sectional views of prototype MR clutch.

where T_1 and T_2 are the field-dependant torques produced by clutches C_1 , and C_2 , respectively, given by

$$T_{i} = \frac{4\pi}{3} \tau_{y}(\mathbf{H}_{i}) \left(R_{2}^{3} - R_{1}^{3}\right) \operatorname{sgn}(\omega_{i}), \quad i = 1, 2$$
(30)

where \mathbf{H}_1 and \mathbf{H}_2 are the fields produced in clutches C_1 , and C_2 , respectively. Note that the individual viscous torque contributions of C_1 and C_2 negate each other at the joint when $\omega_j = 0$. Viscosity of this class of fluids does not always obey ideal models. The antagonistic configuration can mitigate some nonlinearities which would otherwise have to be compensated for by the controller.

559 VI. PERFORMANCE VALIDATION OF A PROTOTYPE MR CLUTCH

560 In this section, we present results obtained by experimentation with a prototype MR clutch which we have designed 561 and constructed (see Fig. 9). The configuration of the prototype 562 MR clutch deviates from the model of Section IV. The magnetic 563 coil of the prototype is located radially inward of the clutch pack 564 in a "coil-in" configuration, as opposed to the coil-out config-565 uration previously discussed. Coupling the coil to the output 566 shaft has the intended effect of reducing clutch mass, however 567 comes at the expense of increasing output inertia. Design of 568 the prototype clutch is partially automated using the optimiza-569 tion process discussed in Section IV-B, where model equations 570 have been updated to reflect the change in configuration. The 571 method returns values for the dimensional parameters that min-572 imize the clutch mass for a given design torque. The prototype 573 MR clutch was specified with a design torque of 120 Nm. The 574 dimensional parameters returned by the optimization process 575 were used as the basis for practical design. Table II compares 576 the output torque, inertia, and mass of the physical prototype 577 MR clutch to the optimized design model. A large discrepancy 578 exists between the modeled and actual torque. The discrepancy 579 results primarily due to deviations in the physical design from 580 the geometric model used in the optimization. Practical design 581 features required for fastening and wire access are omitted from 582 the model. The optimization produces geometries in which flux 583 members enter magnetic saturation at the magnitude of circuit 584 flux corresponding to the specified design torque of the clutch. 585 586 Removal of ferromagnetic material from the optimized geom-

TABLE II Comparison Between Prototype and Modeled MR Clutch, as Well as Commercially Available Servomotors

		Prototype MR Clutch		Servomotors	
	Coil-out	Model	Actual	Parker	Maxon
	n		SMH-100	EC60	
Output Torque[Nm]	75	120	75	6.0	0.83
Mass[kg]	2.8	4.7	4.5	4.7	2.5
Inertia×10 ³ [kg·m ²]	0.19	2.8	5.0	0.34	0.083
Reflected					
Inertia $\times 10^3 [\text{kg} \cdot \text{m}^2]^{\dagger}$	-	-	2.22	23.3	302
[†] Reflected torque T' –	50 Nm				

Reflected torque $T_c' = 50$ Nm.



Fig. 10. Experimental setup used to verify the prototype MR clutch.

etry subsequently results in premature saturation of the circuit, 587 limiting the output torque of the clutch. 588

Much of our analysis prior to this section is based on the coil-589 out configuration model of Section IV-B. To add perspective, we 590 compare this model to the prototype MR clutch. The values for 591 the coil-out configuration shown in Table II are produced with 592 the geometric model and procedure described in Section IV-B, 593 where the output torque is specified to match the constructed 594 MR clutch and not the design value. The coil-out model does 595 not consider any practical design requirements, such as bearings, 596 seals, and mechanical coupling of the disks. In this regard, the 597 model represents an ideal scenario, or baseline for the achievable 598 characteristics in its configuration. The comparison indicates 599 that there is room for improvement of the prototype MR clutch. 600 Ideally, mass could be reduced by a third, while the output inertia 601 might be improved by an order of magnitude. Table II compares 602 the prototype MR clutch to two commercially available servo 603 motors. The servo motors are chosen to have comparable mass to 604 the prototype MR clutch. The output inertia of the servo motors 605 are between one and two orders of magnitude lower than that 606 of the MR clutch. However, when we consider a hypothetical 607 application requiring a 50-Nm output, the prototype MR clutch 608 posses the more favorable reflected inertia by at least an order 609 of magnitude. 610

To assess its performance characteristics, the clutch is 611 mounted to an experimentation platform (see Fig. 10) that incorporates an angular encoder (Renishaw RM22I) to read the 613 position of the output shaft. A static load cell (Transducer Techniques SBO-1K) mounts to the output shaft for torque experiments. A servo motor (Maxon EC 60) provides the rotational 616 input to the MR clutch. A PID controller is implemented on a 617



Fig. 11. Torque tracking of step reference.



Fig. 12. Frequency response of the prototype MR clutch.

desktop computer that communicates with the experimentation
platform via a National Instruments (NI USB-6229) multifunction I/O device. The output signal from the PID controller forms
the input signal to the current amplifier of the MR clutch, while
the rotational velocity of the motor is kept constant.

Fig. 11 shows the closed-loop response to a step input. The 623 rise time is determined to be approximately 10 ms. The fre-624 quency response and dynamic characteristics are examined by 625 measuring the torque response to a sinusoidal reference signal 626 and initiating a frequency sweep at 0.5 Hz. Fig. 12 shows the 627 frequency response of the system. The resulting 3-dB actuator O5 628 bandwidth is measured to be approximately 30 Hz. Fig. 13 629 presents a set of four time domain measurements from the 630 sweep. Beginning at 0.5 Hz, we note excellent overlay of the 631 measured signal with that of the command. As the reference fre-632 quency is increased toward and above the actuator bandwidth, 633 we note that the response remains very smooth and as well re-634 tains the shape of the command signal quite well. Clean and 635 predictable torque outputs are an asset to the development of 636 controls and sensorization schemes that are required to monitor 637 and control contact forces between manipulators and humans. 638

Trajectory tracking experiments were conducted using the 639 angular encoder to form the feedback signal. The motor output 640 was held at a constant rotational velocity. A 50-cm long arm 641 constructed of medium density plastic was coupled to the out-642 put shaft. A counter weight of approximately 2 kg was mounted 643 to the end of arm. The results shown in Fig. 14 indicate the ca-644 pacity of the MR clutch in this arrangement to achieve favorable 645 precision in position control tasks. Small fluctuation errors in 646 the static portions of the trajectory demonstrate the capability 647



Fig. 13. Torque tracking of a sinusoidal references at frequencies of 0.5, 4.0, 16.0, and 33.3 Hz (from top to bottom).



Fig. 14. Position tracking of a trajectory reference. The center plot magnifies the trajectory in the region marked by the dotted red bounding box.

of the MR clutch to suppress fluctuations present in the input 648 drive. 649

MR fluids exhibit promising characteristics for applications 651 in robotics. Specifically, they are well-suited for actuation sys-652 tems developed to interact physically with humans. As we have 653 shown, MR-clutch-based actuators demonstrate excellent torque 654 to mass, and torque to inertia characteristics. This is especially 655 evident for clutches having large torque capacities. This cre-656 ates a niche opportunity for MR-based actuators to be devel-657 oped into light-weight direct-drive (DD) systems. Light-weight 658

DD systems exhibit several characteristics that are sought af-659 ter for human-friendly manipulators, namely: intrinsic back-660 drivability, low output inertia, superior performance and band-661 662 width, as well as high precision in the control of output torque. 663 Furthermore, MR-based actuators can potentially reduce system complexity. Potentially, the accuracy of torque transmis-664 sion models in such systems could allow for high fidelity torque 665 control without the requirement for torque sensors at the joints. 666 This is in contrast to the increasingly complex actuation solu-667 668 tions proposed to deal with physical human interaction.

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